

**Supermassive Dark Stars:  
improved models and first pulsation results**  
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# Prerequisite: self-annihilating dark matter

- **Self-annihilating dark matter (DM):**
  - if DM particle is its own anti-particle
    - ) WIMPs (lightest SUSY particles; Kaluza-Klein particles, sterile neutrinos)
  - self-annihilation gives correct relic density of DM
  - possibly already indirect detection signatures (FERMI-LAT, AMS)
- **Self-annihilation produces heat**
  - **affecting stellar evolution**
    - .) present-day stars: constrained by observations
    - .) first stars: yet unconstrained
  - DM may give rise to an entirely new class of stellar object:
    - “Dark star”**: star of primordial composition, but powered by the heat released due to DM self-annihilation

# First Stars

- First stars form in the high-DM density peaks of primordial (mini-)halos with  $10^{5-6} M_{\text{sun}}$  at high redshift  
 $z \sim 15-25$
- Those halos arose from the merging of smaller structures as overdense regions in the Universe assemble hierarchically into ever larger halos
- Pristine atomic gas of hydrogen and helium
- Baryonic matter cools and collapses via molecular hydrogen cooling into a single small protostar at the center of the halo

# The Dark Star Proposal:

Spolyar, Freese & Gondolo (2008)

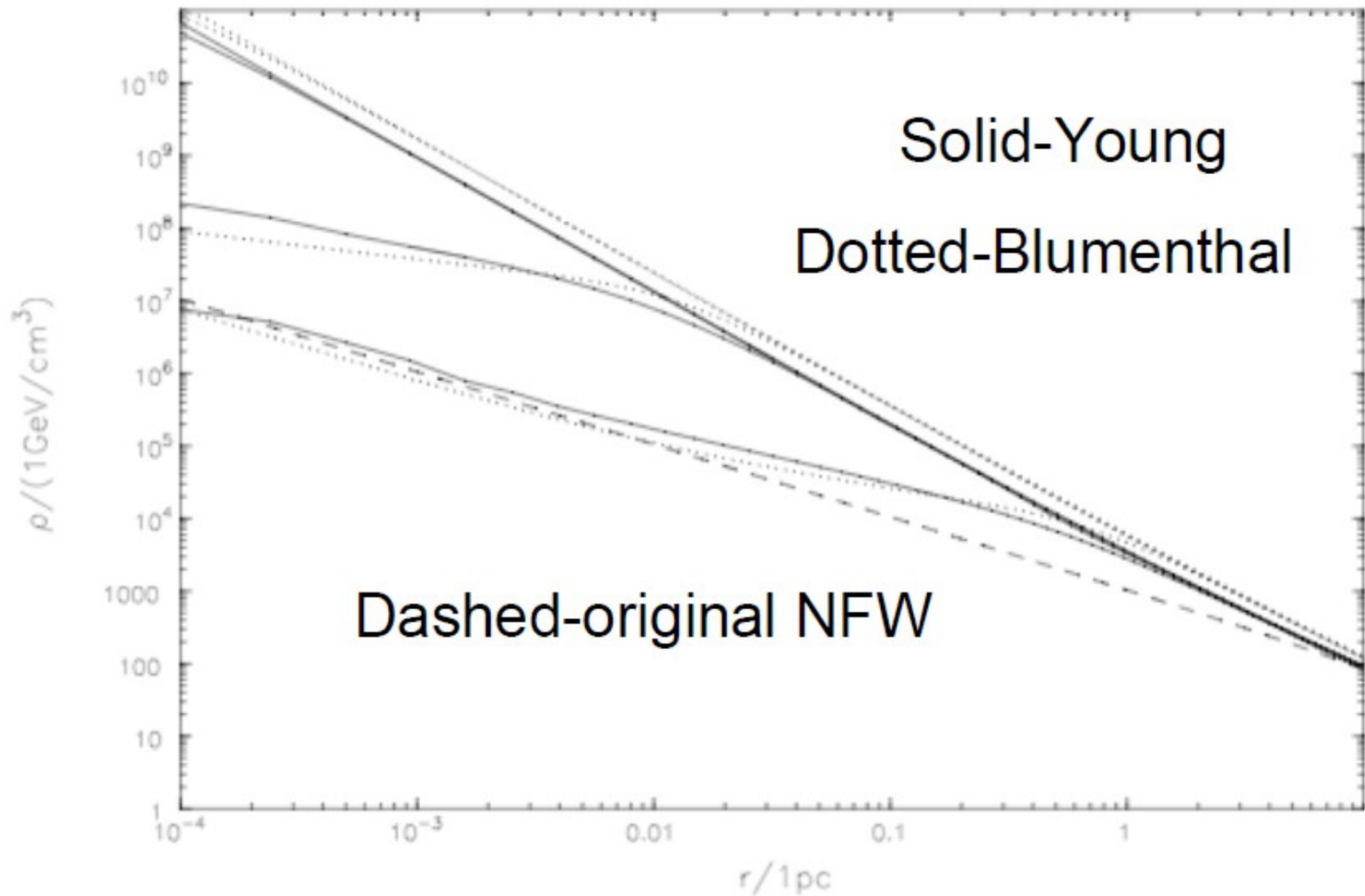
The effect of DM heating is more pronounced at the time when first stars form:

- DM density scales as  $(1+z)^3$
- Protostar forms in the center of minihalo

Supply for DM “fuel”:

- upon collapse, baryons pull in more DM via extended, adiabatic contraction
- at high enough densities, DM replenished by capture from the surroundings, as DM scatters elastically off of nuclei in the star

# Enhanced DM density due to adiabatic contraction



# DM heating

DM annihilation rate:  $n_\chi^2 \langle \sigma v \rangle$

DM **annihilation** produces **energy** at a rate per unit volume

$$\hat{Q}_{DM} = n_\chi^2 \langle \sigma v \rangle m_\chi = \langle \sigma v \rangle \rho_\chi^2 / m_\chi$$

and we take the standard annihilation cross section  $\langle \sigma v \rangle = 3 \times 10^{-26} \text{cm}^3/\text{s}$

Studying a wide range of DM masses is comparable to studying a range of annihilation cross sections

Typical annih.products:  $e^-, \gamma, \nu$

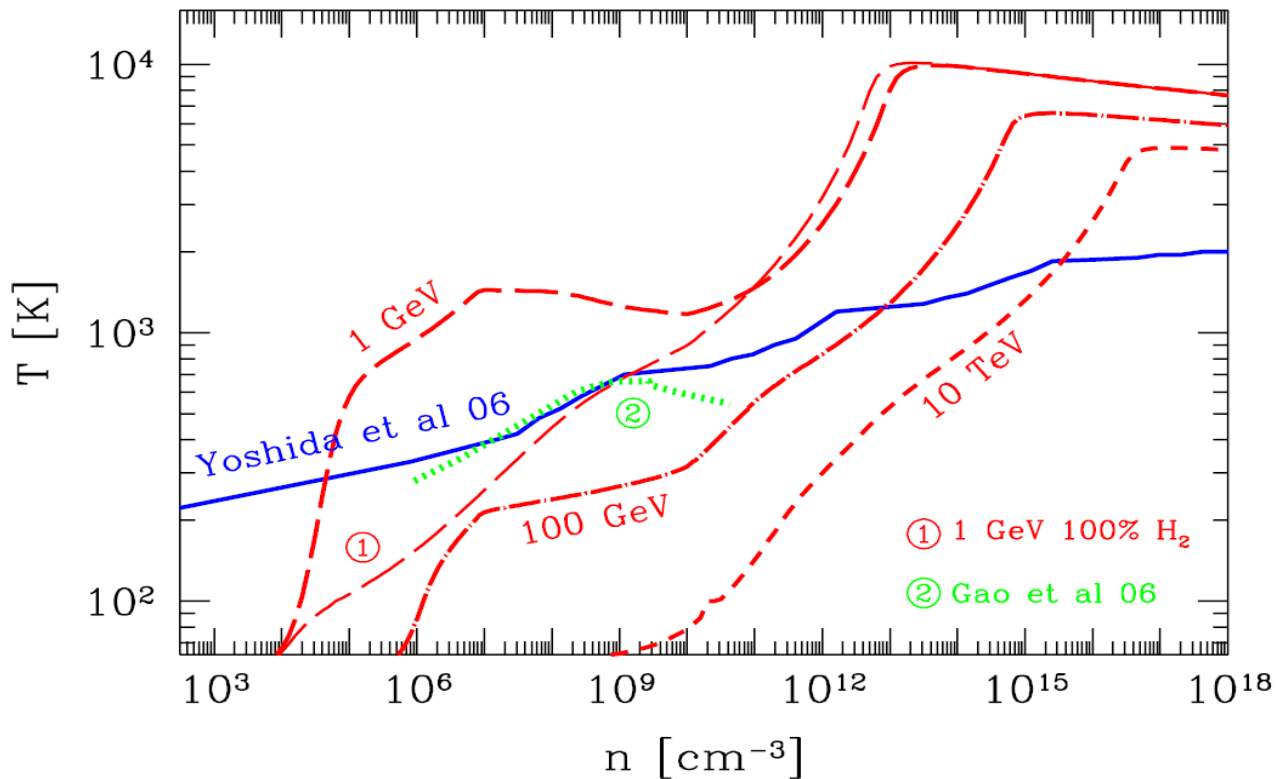
**Luminosity from DM heating:**  $L \sim f_Q \int \hat{Q}_{DM} dV$

$f_Q$  fraction of annh.energy deposited in the star; we take  $f_Q = 2/3$ , as is typical for WIMPs (i.e. DM heating is 67% efficient; compared to 0.07% efficiency for hydrogen fusion)

# The Dark Star Proposal:

Spolyar, Freese & Gondolo (2008)

Critical temperature  $T_c(n)$  below which DM heating dominates over all cooling mechanism ( $H_2$  cooling, H line cooling, Compton cooling) at a given gas density  $n$  of the molecular cloud core



# The Dark Star Proposal:

Spolyar, Freese & Gondolo (2008)

- At sufficiently high densities, most of the annihilation energy is trapped inside the core and heats it up

- **When:**

$$m_{\chi} \approx 1 \text{ GeV} \quad \rightarrow \quad n \approx 10^9 / \text{cm}^3$$

$$m_{\chi} \approx 100 \text{ GeV} \quad \rightarrow \quad n \approx 10^{13} / \text{cm}^3$$

$$m_{\chi} \approx 10 \text{ TeV} \quad \rightarrow \quad n \approx 10^{15-16} / \text{cm}^3$$

- The DM heating dominates over all cooling mechanisms, impeding the further collapse of the core



How does this affect the subsequent evolution of the star ?

What equilibrium structure results ?

# Equations of stellar structure in 1D

$$\frac{dM(r)}{dr} = 4\pi r^2 \rho(r) \quad \text{conservation of mass}$$

$$\frac{dL(r)}{dr} = 4\pi r^2 \rho(r) \epsilon(r) \quad \text{conservation of energy}$$

$$\frac{dP(r)}{dr} = -\frac{GM(r)\rho(r)}{r^2} \quad \text{conservation of momentum (=hydrostatic equilibrium)}$$

$$\frac{dT(r)}{dr} = -\frac{3\kappa(r)\rho(r)L(r)}{16\pi acT^3(r)r^2} \quad \text{radiative transport}$$

$$\left(\frac{dT(r)}{dr}\right)_{ad} = \frac{\mu m_h GM(r)}{(n+1)kr^2} \quad \text{convective transport}$$

$$(\Delta \nabla T) = \left[ \frac{L^2(r)T(r)}{C_p^2 \rho^2(r) GM(r) \pi^2 l^4 r^2} \right]^{1/3}$$

# Equations of stellar structure in 1D

$$\epsilon = \epsilon[T(r), \rho(r), \mu(r)] \quad \text{energy production}$$

$$\kappa = \kappa[T(r), \rho(r), \mu(r)] \quad \text{radiative opacity}$$

$$\gamma = \gamma[T(r), \rho(r), \mu(r)] \quad \text{adiabatic index}$$

$$P = P[T(r), \rho(r), \mu(r)] \quad \text{equation of state}$$

# Supermassive Dark Stars: stellar evolution using polytropes

(Freese, Ilie, Spolyar, Valluri, Bodenheimer, 2010)

Assume that DS can be described using polytropic law

$P = K\rho^{1+1/n}$  in hydrostatic equilibrium:

grow DS and calculate new equilibria iteratively during its evolution

→ established that DS can grow to **supermassive size**

with masses  $M \sim 10^4 - 10^7 M_{\text{sun}}$

having luminosities  $L \sim 10^9 - 10^{11} L_{\text{sun}}$

→ good prospects of observing them with JWST

# Dark Star evolution: improved models

Use 1D fully-fledged stellar evolution code

MESA

(**M**odules for **E**xperiments in **S**tellar **A**strophysics)

<http://mesa.sourceforge.net/>

- improve upon polytropic models
- study pulsations of dark stars
- other features in stellar evolution ('flashes')

# Halo environments

- DM: 85 %, baryons: 15 %
- H: 76 %, He: 24 %
- $c = 3.5$

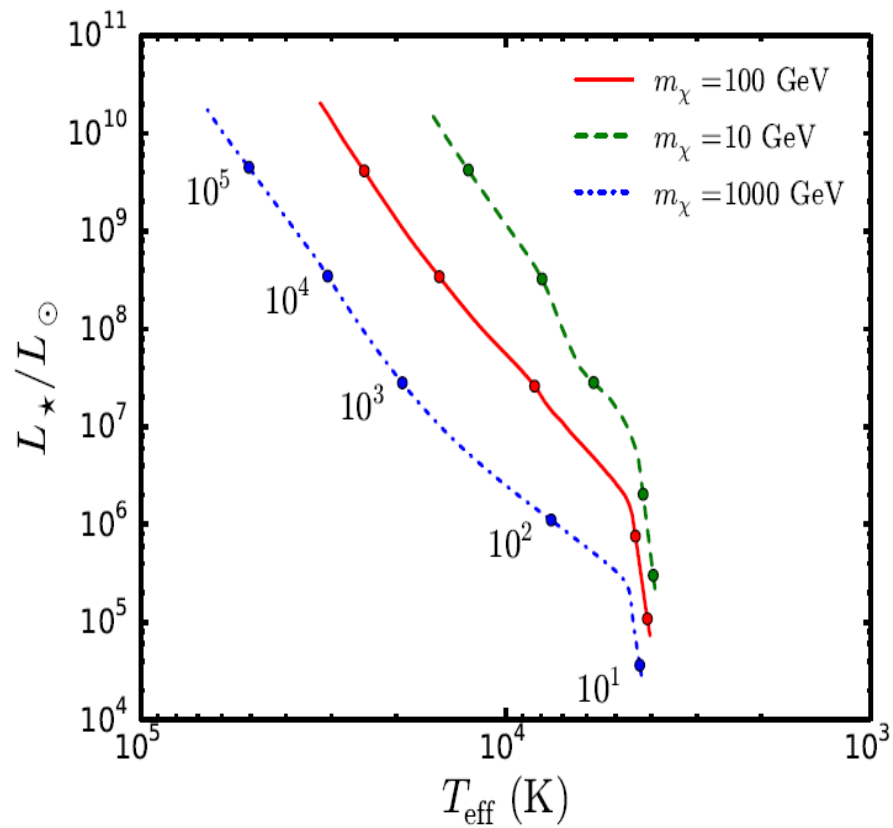
**SMH:** “small halo” : total mass  $10^6 M_{\text{sun}}$  at  $z = 20$ ,  
accretion rate  $dM/dt = 10^{-3} M_{\text{sun}}/\text{yr}$

**LMH:** “large halo” : total mass  $10^8 M_{\text{sun}}$  at  $z = 15$ ,  
accretion rate  $dM/dt = 10^{-1} M_{\text{sun}}/\text{yr}$

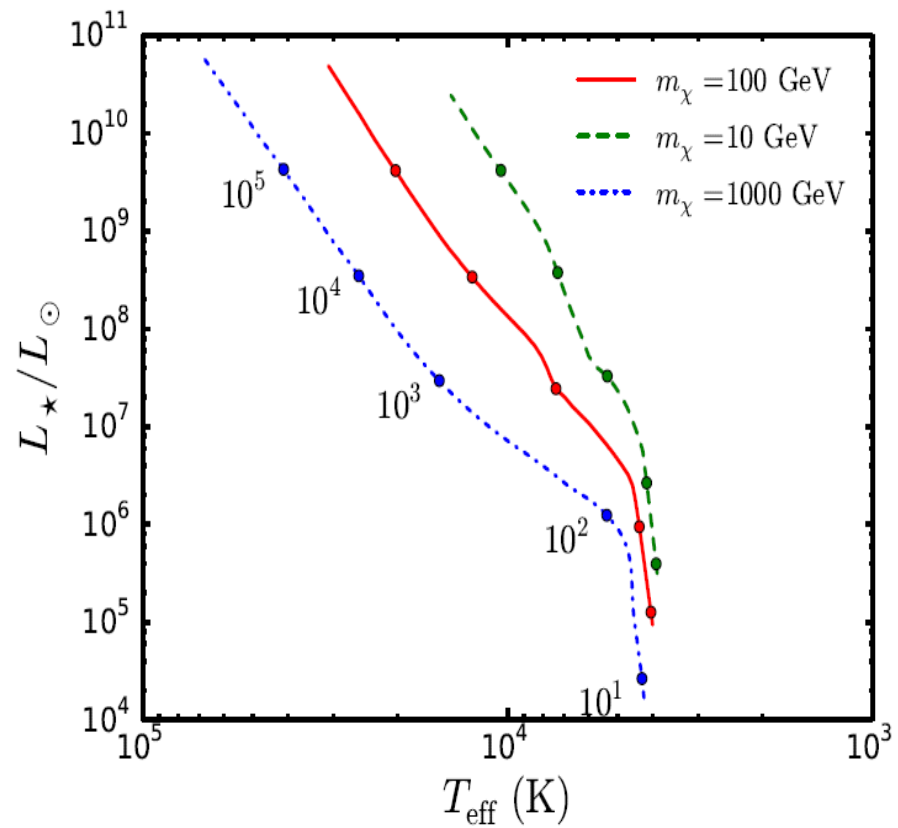
for  $m_\chi = 10, 100, 1000 \text{ GeV}$

# Tracks in the Hertzsprung-Russell Diagram

SMH



LMH



# Main stellar characteristics

MESA dark stars with  $10^4 - 10^6 M_{\text{sun}}$  are

- brighter  $\sim 2x$
- hotter  $\sim 1.5x$  (for  $T_{\text{eff}}$  and  $T_c$ )
- smaller  $\sim 0.6x$
- denser  $\sim 3-4 x$

than polytropic DS models of Freese et al (2010)

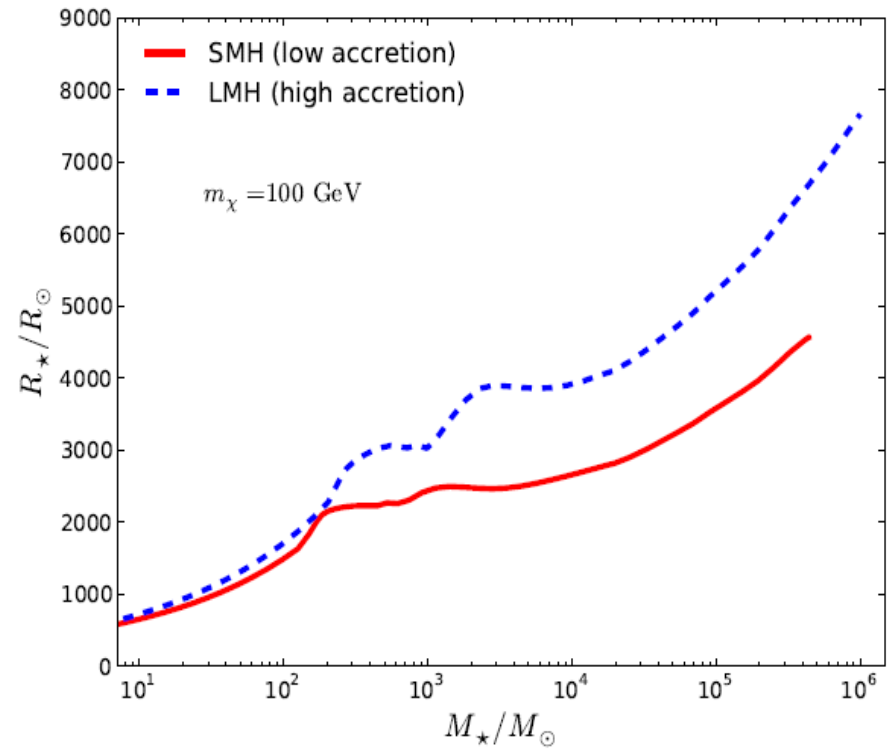
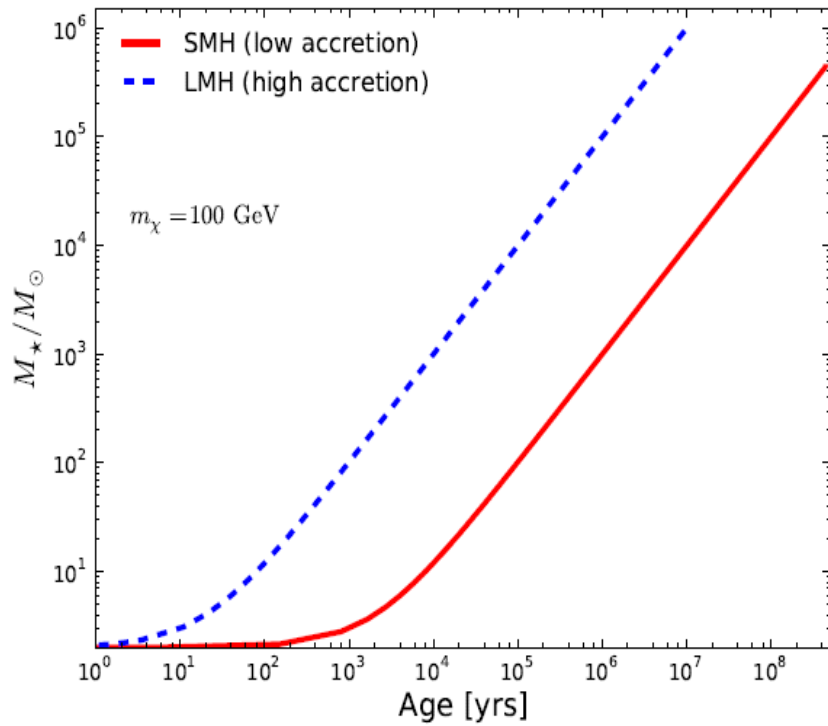


# Focus on **100 GeV** case: Main stellar characteristics

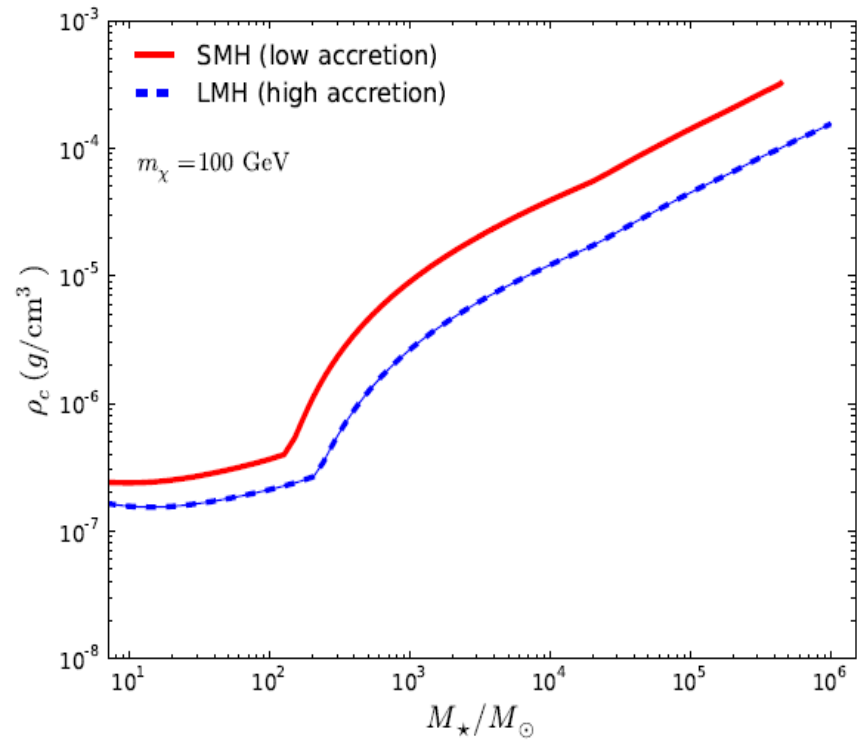
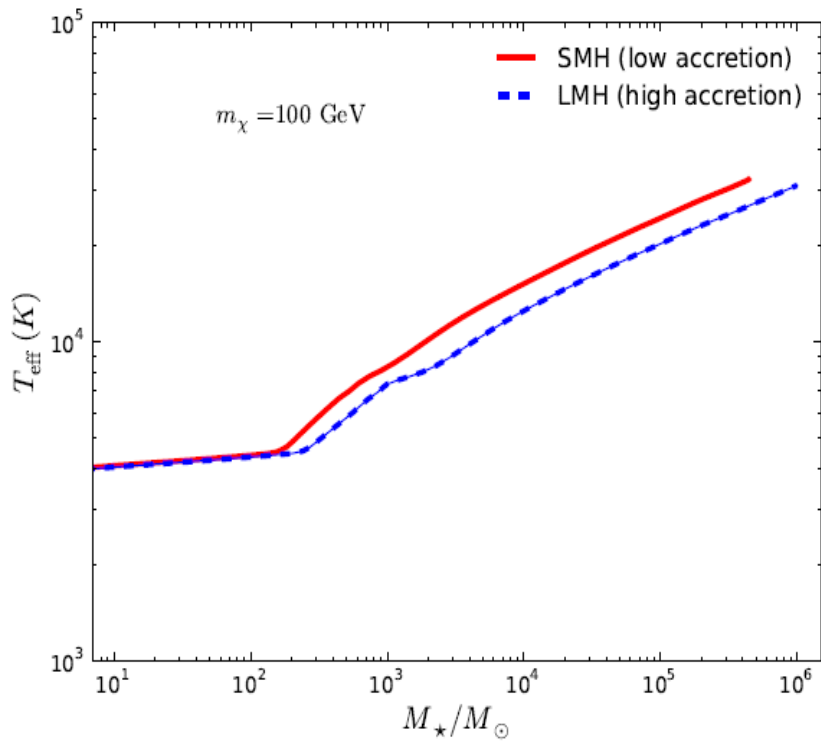
MESA dark stars with  **$10^4$  -  $10^6 M_{\text{sun}}$**  :

	$M_{\star}$ [ $M_{\odot}$ ]	$L_{\star}$ [ $10^6 L_{\odot}$ ]	$R_{\star}$ [ $R_{\odot}$ ]	$T_{\text{eff}}$ [ $10^3$ K]	$T_c$ [ $10^5$ K]	$\rho_c$ [g cm $^{-3}$ ]
SMH:	$10^4$	341.21	2659.2	15.2	30.6	$3.9 \times 10^{-5}$
	$10^5$	4121.02	3578.6	24.4	69.5	$1.4 \times 10^{-4}$
LMH:	$10^4$	338.41	3916.5	12.5	20.7	$1.2 \times 10^{-5}$
	$10^5$	4149.34	5205.5	20.3	47.3	$4.5 \times 10^{-5}$
	$10^6$	48203.79	7797.4	31.4	106.6	$1.6 \times 10^{-4}$

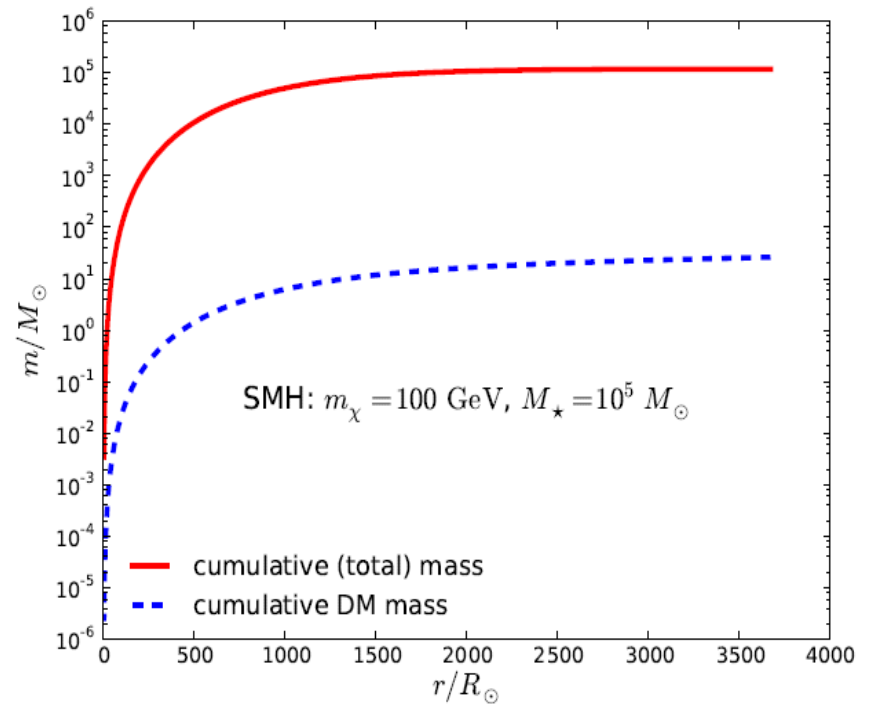
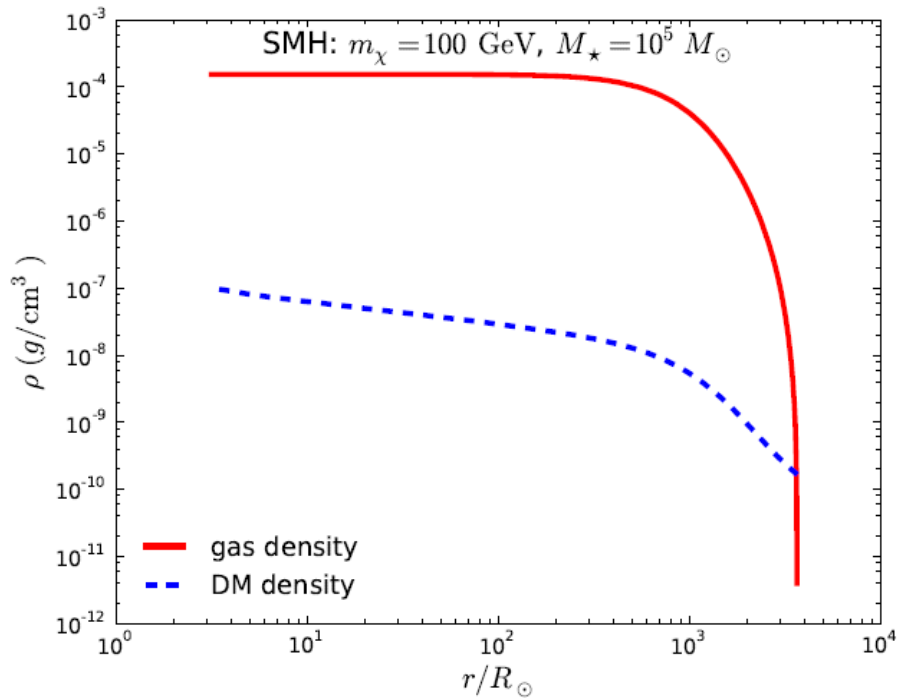
# Evolution of DS



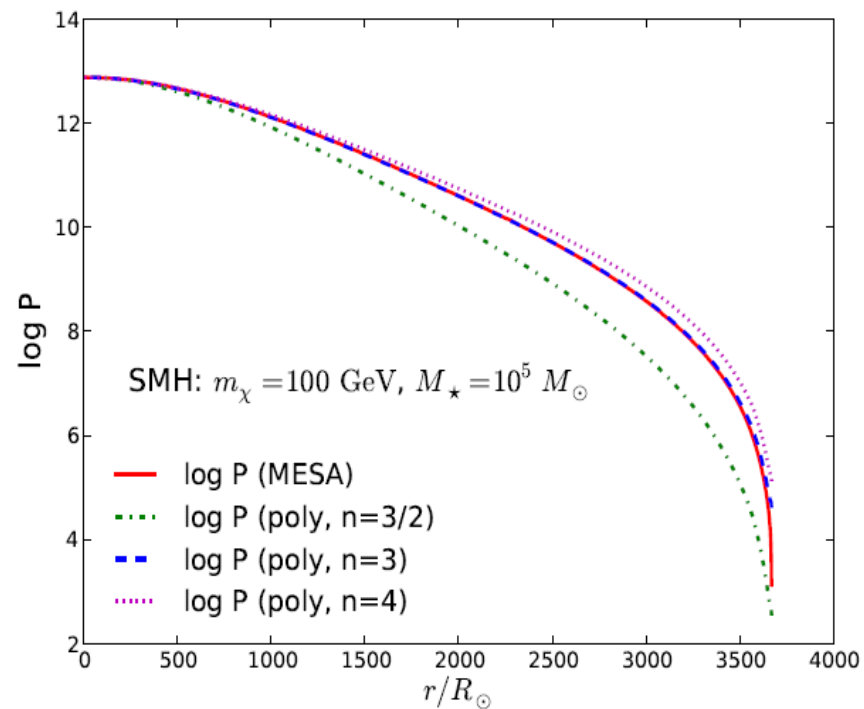
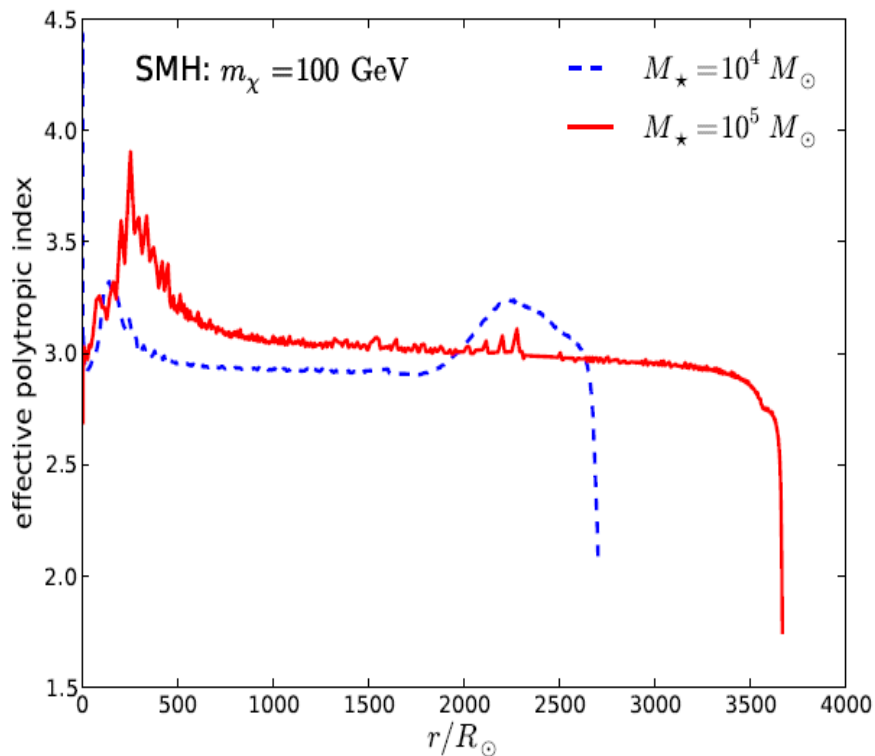
# Evolution of DS (cont.)



# Focus on SMH: density profiles



# Pressure distribution



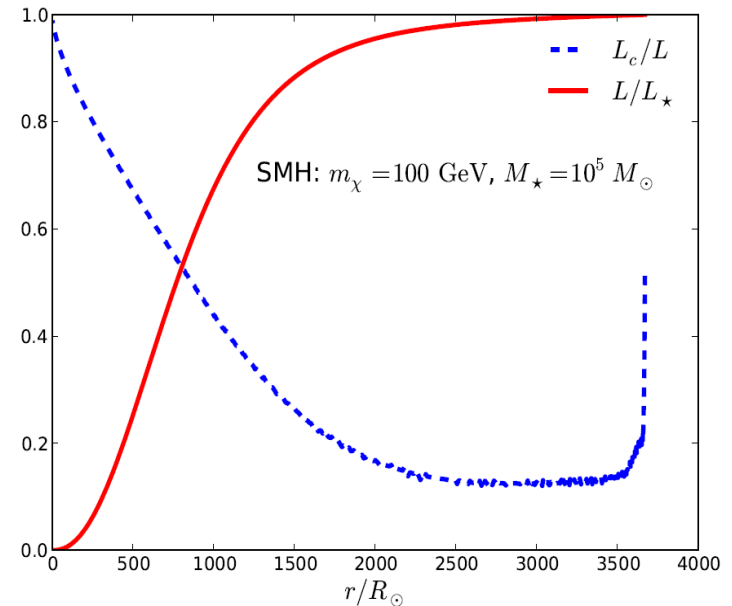
$$n_{\text{eff}} = \left[ \frac{\log(P/P_c)}{\log(\rho/\rho_c)} - 1 \right]^{-1}$$

Supermassive DS can be very well approximated by **(n=3)-polytropes**

# Deviations from equilibrium: pulsations

Energy transport in supermassive DS is dominated by radiation transfer;  
weak convection

→ expect **no gravity modes**  
(or g-modes)



But **acoustic modes (or p-modes) are permitted**

→ calculate adiabatic pulsation periods of radial modes ( $l=0$ )

with different overtone number  $n$ :

$n=1$  fundamental mode;  $n > 1$  higher overtone modes

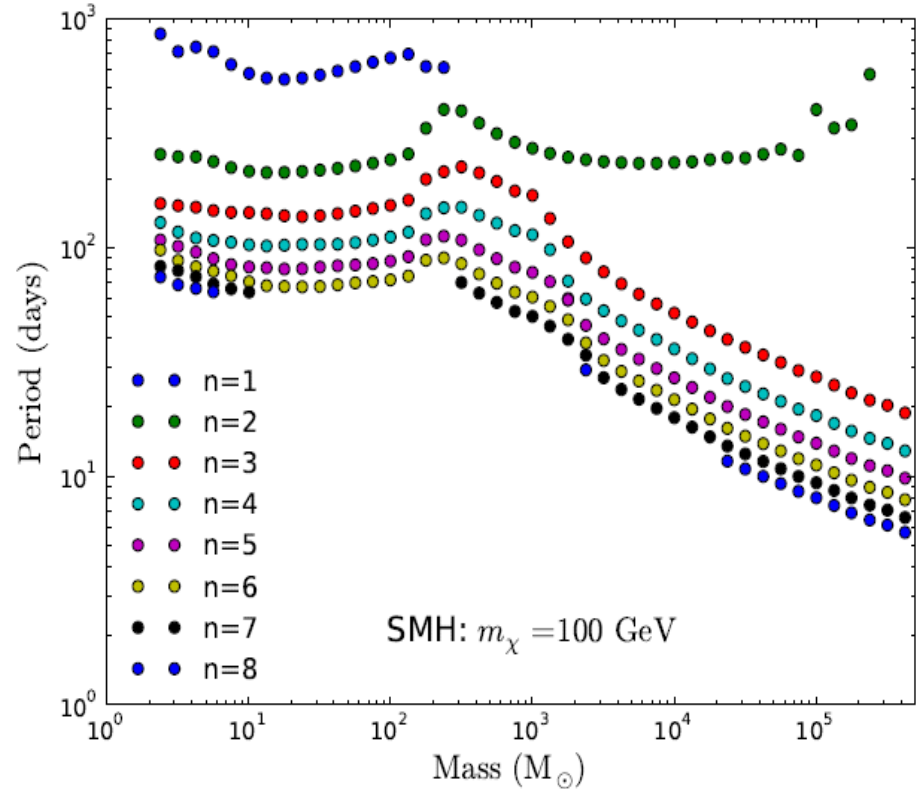
# Pulsation periods of acoustic, or p-modes

$$M_{\star} = 10^5 M_{\odot}$$

$$T_{\text{eff}} = 24463.62 \text{ K}, L_{\star} = 4.150 \cdot 10^9 L_{\odot}, R_{\star} = 3589.72 R_{\odot}$$

$n$	$f$ [ $\mu\text{Hz}$ ]	periods [days]	observer's frame [days]
2	0.02896	399.69	6247.15
3	0.42679	27.12	423.88
4	0.62926	18.39	287.43
5	0.83194	13.91	217.41
6	1.03558	11.18	174.74
7	1.23825	9.35	146.14
8	1.43942	8.04	125.66

- the periods are much shorter for higher  $n$
- more modes with high  $n$  for larger DM mass
- periods are shorter for larger DM mass  
10 GeV: 60-400 days; 1000 GeV:  $\sim O(\text{days})$   
in the rest frame
- shortest periods expected in the observer's frame:  
1000 GeV:  $< 50$  days for modes with  $n > 6$



# Summary

DM may be responsible for an entirely new class of stellar object: “Dark Star”, its luminosity powered by heat released due to DM self-annihilation

→ alter the standard picture of first star formation with implications for reionization, supermassive BH formation, galaxy evolution

→ detectable by JWST

→ if pulsations can be driven, DS might someday serve as novel standard candles for cosmological studies





# Next steps

- study driving mechanisms of pulsation modes of dark stars in more detail
- implement DM capture via nuclei within the DS
- study dark star 'flash' in luminosity when DM runs out

